



SCUOLA
NORMALE
SUPERIORE

SEMINARIO DI MATEMATICA

Martedì 25 giugno 2019
ore 11:00

Scuola Normale Superiore
Pisa
Aula Mancini

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Terrà un seminario dal titolo:

“Crouzeix’s conjecture”

Abstract:

Crouzeix's conjecture is among the most intriguing developments in matrix theory in recent years. Made in 2004 by Michel Crouzeix, it postulates that, for any polynomial p and any matrix A , $\|p(A)\| \leq 2 \max(|p(z)|: z \in W(A))$, where the norm is the 2-norm and $W(A)$ is the field of values (numerical range) of A , that is the set of points attained by v^*Av for some vector v of unit length. Crouzeix proved in 2007 that the inequality above holds if 2 is replaced by 11.08, and recently this was greatly improved by Palencia, replacing 2 by $1+\sqrt{2}$. Furthermore, it is known that the conjecture holds in a number of special cases, including $n=2$. We use nonsmooth optimization to investigate the conjecture numerically by locally minimizing the “Crouzeix ratio”, defined as the quotient with numerator the right-hand side and denominator the left-hand side of the conjectured inequality. We also present local nonsmooth variational analysis of the Crouzeix ratio at conjectured global minimizers. All our results strongly support the truth of Crouzeix’s conjecture.

Tutti gli interessati sono invitati a partecipare.

Classe di Scienze